

YOUNG'S DOUBLES SLIT EXPERIMENT

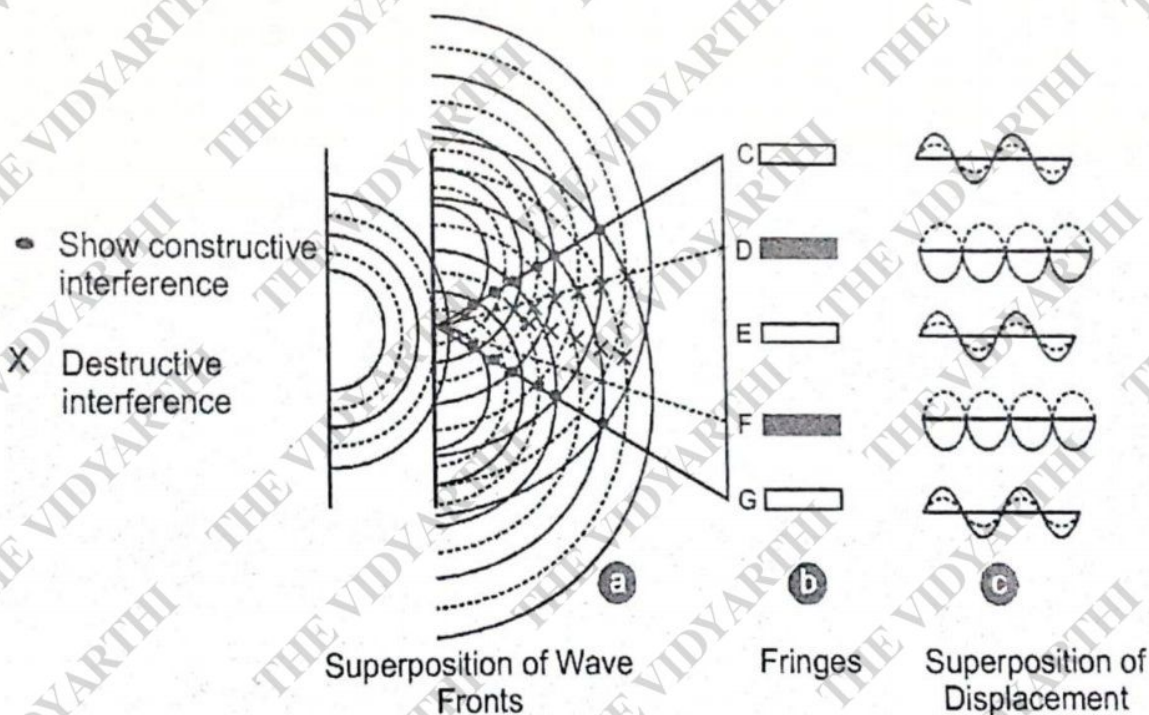
In this experiment a single slit is divided to two slits.

This experiment verifies the wave nature of light.

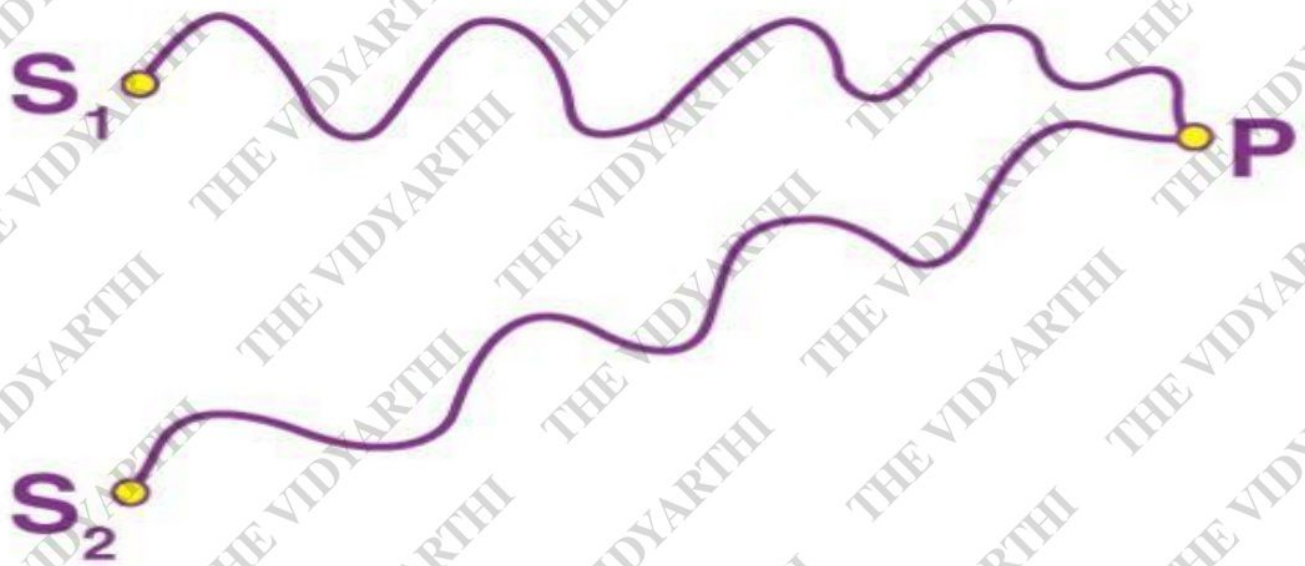
The slit S_1 and S_2 behaves as coherent sources.

The bright and dark fringes are obtained alternately.

The bright fringes are the result of constructive interference where as dark fringes are the Result of destructive interference.



Condition for Constructive and Destructive Interference



Let

The equation of the ray S1-

$$y_1 = a_1 \sin \omega t$$

Equation of the ray S2-

$$y_2 = a_2 \sin(\omega t + \phi)$$

[where ϕ is the phase difference.]

Equation of the resultant ray-

$$y = y_1 + y_2$$

$$y = a_1 \sin \omega t + a_2 \sin(\omega t + \phi)$$

$$y = a_1 \sin \omega t + a_2 \sin \omega t \cos \phi + a_2 \cos \omega t \sin \phi$$

[$\sin(A+B) = \sin A \cos B + \cos A \sin B$]

$$y = \sin \omega t (a_1 + a_2 \cos \phi) + a_2 \sin \phi \cos \omega t$$

Let-

$$(a_1 + a_2 \cos \phi) = A \cos \theta \quad (1)$$

$$a_2 \sin \phi = A \sin \theta \quad (2)$$

$$y = A \sin \omega t \cos \theta + A \sin \theta \cos \omega t$$

$$y = A \sin(\omega t + \theta)$$

Squaring and adding equation (1) and (2)-

$$(a_1 + a_2 \cos \phi)^2 + a_2^2 \sin^2 \phi = A^2 \cos^2 \theta + A^2 \sin^2 \theta$$

$$a_1^2 + a_2^2 \cos^2 \phi + 2a_1 a_2 \cos \phi + a_2^2 \sin^2 \phi = A^2$$

$$a_1^2 + a_2^2 + 2a_1 a_2 \cos \phi = A^2$$

$$\text{Intensity} = K A^2$$

$$\text{Intensity} = K(a_1^2 + a_2^2 + 2a_1 a_2 \cos \phi)$$

So If –

$$\cos \phi = 2n\pi \quad (\text{Constructive Interference})$$

$$\cos \phi = (2n-1)\pi \quad (\text{Destructive Interference})$$