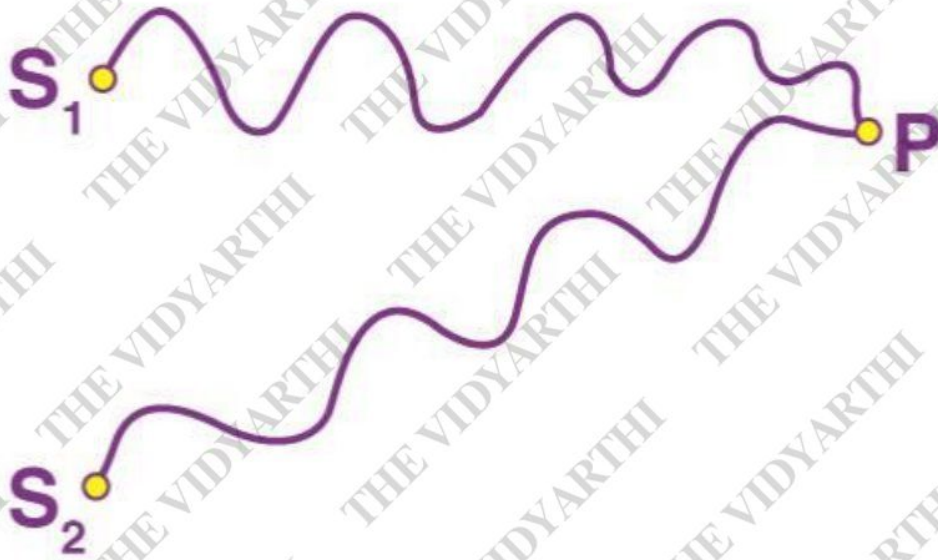


Two coherent sources of Intensity ratio α interfere for the interference pattern. Prove that-

$$I_{\max} - I_{\min} / I_{\max} + I_{\min} = 2\sqrt{\alpha} / 1 + \alpha$$

Where the symbols have the usual meaning.



Intensity of S₁ = I₁

Intensity of S₂ = I₂

[Intensity = K A²]

$$I_1 = K A_1^2$$

$$I_2 = K A_2^2$$

$$I_1 / I_2 = A_1^2 / A_2^2 = \alpha$$

LHS

$$= (I_2 + I_1) - (I_2 - I_1) / (I_2 + I_1) + (I_2 - I_1)$$

$$= (A_2 + A_1)^2 - (A_2 - A_1)^2 / (A_2 + A_1)^2 + (A_2 - A_1)^2$$

$$= A_2^2 + A_1^2 + 2A_1A_2 - A_2^2 - A_1^2 + 2A_1A_2 / A_2^2 + A_1^2 + 2A_1A_2$$

$$+ A_2^2 + A_1^2 - 2A_1A_2$$

$$= 4A_1A_2 / 2(A_2^2 + A_1^2)$$

$$= 2A_1A_2 / A_2^2 + A_1^2$$

Dividing the equation with A_2^2 -

$$= 2(A_1/A_2) / 1 + (A_1^2/A_2^2)$$

$$= 2\sqrt{\alpha} / 1 + \alpha$$

RHS